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# Proteins - a celebration of consilience 

physics meets biology

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## AlphaFold: Breakthrough of the Year 2021

## Science



## Article <br> Highly accurate protein structure prediction with AlphaFold

| https://doi.org/10.1038/s41586-021-03819-2 | John Jumper ${ }^{14 \boxtimes}$, Richard Evans ${ }^{14}$, Alexander Pritzel ${ }^{[1,4}$, Tim Green ${ }^{14}$, Michael Figurnov ${ }^{1,4}$, Olaf Ronneberger ${ }^{1,4}$, Kathryn Tunyasuvunakool ${ }^{1,4,}$, Russ Bates ${ }^{14}$, Augustin Židek ${ }^{1,4}$, Anna Potapenko ${ }^{1,4}$, Alex Bridgland ${ }^{1,4}$, Clemens Meyer ${ }^{14}$, Simon A. A. Kohl ${ }^{1,4,}$, <br> Andrew J. Ballard ${ }^{14,}$, Andrew Cowie ${ }^{1,4}$, Bernardino Romera-Paredes ${ }^{1,4}$, Stanislav Nikolov ${ }^{1,4}$, Rishub Jain ${ }^{1 / 4}$, Jonas Adler ${ }^{1}$, Trevor Back ${ }^{1}$, Stig Petersen ${ }^{1}$, David Reiman ${ }^{1}$, Ellen Clancy ${ }^{1}$, <br> Michal Zielinski', Martin Steinegger ${ }^{233}$, Michalina Pacholska', Tamas Berghammer ${ }^{1}$, <br> Sebastian Bodenstein ${ }^{1}$, David Silver ${ }^{1}$, Oriol Vinyals ${ }^{1}$, Andrew W. Senior ${ }^{1}$, Koray Kavukcuoglu ${ }^{1}$, <br> Pushmeet Kohli' \& Demis Hassabis ${ }^{1,4}$ |  |  |
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## Is protein folding problem solved?

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| （⿴囗十）Check for updates | Pushmeet Kohti＇\＆Demis Hassab |

## Is protein folding problem solved？

## The protein－folding problem：Not yet solved

We agree with H．H．Thorp（＂Proteins，pro－ teins everywhere，＂Editorial， 17 December 2021，p．1415）and numerous others（ 1 ）that the advance in protein structure predic－ tion achieved by the computer programs AlphaFold（2）and RoseTTAfold（3）is worthy of special notice．The accuracies of the predictions afforded by these new approaches，which use machine－learning methods that exploit the information about the relationship between sequence and structure contained in the databases of experimental protein structures and sequences，are much superior to previous approaches．However，we do not agree with Thorp that the protein－folding problem has been solved．

## Not yet，so let＇s keep doing it！

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## A brief introduction to proteins

- Linear chains (of amino acids) with bond length $\sim 3.8 \AA$
- 20 amino acid types with distinct side chains
- Proteins fold rapidly and reproducibly (Anfinsen)
- Textbook paradigm: sequence determines structure
- Folding driven by hydrophobicity $\rightarrow$ protein maximizes self-interaction \& expels water from its interior
- Space-filling building blocks: $\alpha$ - helices and almost planar $\beta$ - sheets
- Modular structure, finite number of folds



## Linus Pauling

- Geometries of protein building blocks predicted from quantum chemistry: planarity of the peptide bond \& need for a coherent placement of hydrogen bonds

THE STRUCTURE OF PROTEINS: TWO HYDROGEN-BONDED HELICAL CONFIGURATIONS OF THE POLYPEPTIDE CHAIN

By Linus Pauling, Robert B. Corey, and H. R. Branson*
Gates and Crellin Laboratories of Chemistry,
California Institute of Technology, Pasadena, California $\dagger$
Communicated February 28, 1951


CONFIGURATIONS OF POLYPEPTIDE CHAINS WITH FA VORED ORIENTATIONS AROUND SINGLE BONDS: TWO NEW PLEATED SHEETS
By Linus Pauling and Robert B. Corey
Gates and Crbllin Laboratoribs of Chbmistry,* California Institute of Technology, Pasadena, California

Communicated September 4, 1951


A diagrammatic representation of the parallel-chain pleated sheet structure.



FIGURE 4


A diagrammatic representation of the antiparallel-chain pleated sheet structure.

## Polymers vs. Proteins



## What is missing?

## Amino acid heterogeneity? Chemistry?

Or does one need to remove spurious symmetries?

## Breaking spherical symmetry

- Chain is uniaxial This inconsistency can be
e Sphere is isotropic $\int$ removed by overlap

+ effective attraction mimicking hydrophobic collapse $+\underline{\text { side spheres }}$ in anti-normal direction (steric hindrance)


## Elixir phase



Škrbić, Hoang, Maritan, Banavar \& Giacometti, Proteins (2019) Škrbić, Hoang, Maritan, Banavar \& Giacometti, Soft Matter (2019)


- When inspected carefully, helices \& sheets do not have the right geometries
e Breaking spherical symmetry helps


## But what is missing?

## Space-filling is not correctly captured!

$$
\dot{\stackrel{2}{2}}
$$

Continuum case
a)

b)


Maritan, Micheletti,
Trovato \& Banavar, Nature (2000)

## The discrete

 space-filling helix- Bond length equal to $3.81 \AA$
- Space-filling discrete helix determined from elementary mathematics \& physics

Tube radius $\underline{\Delta} \approx 2.63 \AA$

Rotation angle $\varepsilon \approx 99.8^{\circ}$

Pitch to radius ratio

$$
\eta=P /(2 \pi R) \approx 0.400
$$

$$
\varepsilon \sim 99.8^{\circ}
$$

## Discreteness: $\beta$-strands

$$
r(t)=R(\sin t, \cos t, \eta t)
$$

$\varepsilon$ is rotation angle
$\mathrm{t}=\mathrm{n} \varepsilon, \mathrm{n}=1,2,3, \ldots$
$\mathbf{R}=$ helix radius
$\mathrm{P}=$ helix pitch
$\eta=P /(2 \pi R)$

- Three distinct geometries
- Discreteness enables a second building block



## Two types of assembly of $\beta$-strands



## Tube radius of $2.63 \AA ̊$



## Experimental data on more than 4000 protein structures from PDB are in accord with zero-parameter theory



| HELIX | Theory | PDB data |
| :--- | :--- | :---: |
| Rotation angle $\varepsilon\left[^{\circ}\right]$ | $\underline{99.8}$ | $99.1 \pm 3.4$ |
| \# of residues per turn | $\underline{3.61}$ | $3.63 \pm 0.13$ |
| Helix radius R $[\AA]$ | $\underline{2.27}$ | $2.30 \pm 0.07$ |
| Helix pitch P $[\AA]$ | $\underline{5.69}$ | $5.47 \pm 0.49$ |
| Ratio $\eta=\mathrm{P} /(2 \pi \mathrm{R})$ | $\underline{0.400}$ | $0.377 \pm 0.046$ |
| $\angle(i, i+3, i+4)\left[^{\circ}\right]$ | $\underline{90.0}$ | $86.5 \pm 3.9$ |
| $\boldsymbol{d}(\boldsymbol{i}, \boldsymbol{i}+3)[\AA]$ | $\underline{\mathbf{2 \Delta}}=5.26$ | $5.12 \pm 0.16$ |
| $\boldsymbol{\theta}\left[^{\circ}\right]$ | $\underline{91.8}$ | $91.3 \pm 2.2$ |
| $\boldsymbol{\mu}\left[^{\circ}\right]$ | $\underline{\underline{52.4}}$ | $49.7 \pm 3.9$ |

Škrbić, Maritan, Giacometti, Rose \& Banavar, Phys. Rev. E (2021)
Škrbić, Hoang, Giacometti, Maritan \& Banavar, Int. J. Mod. Phys. B (2022)

## Experimental data on more than 4000 protein structures from PDB are in accord with zero-parameter theory

$\beta \uparrow \uparrow$


| SHEET | Theory | PDB data |  |
| :--- | :---: | :---: | :---: |
| Parallel $\beta$-sheet |  |  |  |
| $\boldsymbol{\theta}\left[\left[^{\circ}\right]\right.$ | $\underline{\text { flexible }}$ | $121 \pm 10$ |  |
| $\boldsymbol{\mu}\left[^{\circ}\right]$ | $\underline{\sim 180}$ | $191 \pm 17$ |  |
| $\boldsymbol{d}\left(\boldsymbol{i}+1, M_{j+1}\right)[\AA]$ | $\underline{2 \Delta=5.26}$ | $5.26 \pm 0.16$ |  |
| $\angle\left(\boldsymbol{i}-1, M_{j-1}, M_{j+1}\right)\left[^{\circ}\right]$ | $\underline{90.0}$ | $87.2 \pm 4.5$ |  |
| $\angle\left(M_{j-1}, i-1, i+1\right)\left[{ }^{\circ}\right]$ | $\underline{90.0}$ | $87.6 \pm 3.6$ |  |

Škrbić, Maritan, Giacometti, Rose \& Banavar, Phys. Rev. E (2021)
Škrbić, Hoang, Giacometti, Maritan \& Banavar, Int. J. Mod. Phys. B (2022)

## Experimental data on more than 4000 protein structures from PDB are in accord with zero-parameter theory

$\beta \uparrow \downarrow$


| SHEET | Theory |  |
| :--- | :---: | :--- |
| PDB data |  |  |
|  | Antiparallel $\beta$-sheet |  |
| $\boldsymbol{\theta}\left[^{\circ}\right]$ | $\underline{\text { flexible }}$ | $127 \pm 10$ |
| $\boldsymbol{\mu}\left[^{\circ}\right]$ | $\underline{\sim 180}$ | $186 \pm 20$ |
| $\boldsymbol{d}(\boldsymbol{i}, \boldsymbol{j})[\AA]$ | $\underline{2 \Delta=5.26}$ | $5.26 \pm 0.20$ |
| $\angle(i-1, j+1, j+3)\left[^{\circ}\right] \underline{90.0}$ | $87.0 \pm 4.2$ |  |
| $\angle(j+1, i-1, i+1)\left[^{\circ}\right] \underline{90.0}$ | $86.4 \pm 4.1$ |  |

# Textbook paradigm: Sequence determines structure 

$\square$

## Sequence selects structure

from the menu of pre-determined folds: Sequence independent free energy landscape

- Banavar, Maritan et al. (2000 onwards)

Finite \# of distinct folds
( $\sim 10,000$ structures in PDB)
Homopolymer:
all minima are equivalent
vs.

Astronomical \# of putative sequences ( $\sim 100{ }^{20}$ )

Specific sequence: one minimum is selected

## Summary

* First principles, zero parameter predictions of protein building blocks geometries validated by experimental structures
* Discreteness is essential for life
* Possibility of new classes of protein-like nano-machines not necessarily based on carbon chemistry
* While sequences and functionalities undergo Darwinian evolution, protein structures are Platonic and immutable - this helps maintain functionality during evolution
* Future investigation: understanding the role of amino acid specificity in dictating the choice of the native state fold
* Consilience: Chemistry \& Biology provide a perfect fit to the dictates of Mathematics \& Physics

